

OVERVIEW OF RESUMMATION

STEFANO FORTE
UNIVERSITÀ DI MILANO & INFN



UNIVERSITÀ DEGLI STUDI DI MILANO
DIPARTIMENTO DI FISICA

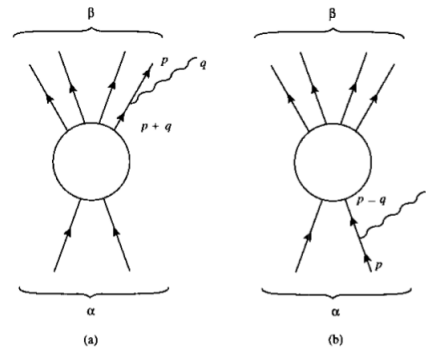


PARTON SHOWERS AND
RESUMMATION

LUND, JUNE 4, 2018

15th-17th July 2013

WHERE IT ALL COMES FROM: EIKONAL EMISSION...



EMISSION OF A SOFT ($q^\mu \rightarrow 0$) GAUGE PARTICLE FROM **EXTERNAL LINE**

$$\sigma(\alpha \rightarrow \beta) \rightarrow \sigma(\alpha \rightarrow \beta) \frac{ep^\mu}{p \cdot q - i\epsilon}$$

(Bloch, Nordiseck, 1937; Yenni, Frautschi, Suura, 1955; Weinberg, 1964)

- **SOFT EMISSION** \Rightarrow **EIKONAL FACTOR**
- **CROSS SECTION** FOR SINGLE (DOUBLE. . .) EMISSION **INFRARED DIVERGENT**; **DIVERGENCE CANCELLED** BY VIRTUAL CORRECTIONS
- **1,2,. . . ,N EMISSIONS EXPONENTIATE** $\Rightarrow \Gamma \sim \exp - \left[\alpha \ln^2 \left(1 - \frac{M_\beta^2}{s} \right) \right]$ (Sudakov, 1956)
- AFTER CANCELLATION, **LEFTOVER SOFT LOGS**:

$$\sigma(\alpha \rightarrow \beta) \rightarrow \sigma(\alpha \rightarrow \beta) \ln^2 \left(1 - \frac{M_\beta^2}{s} \right)$$



15th-17th July 2013

...AND RESUMMATION

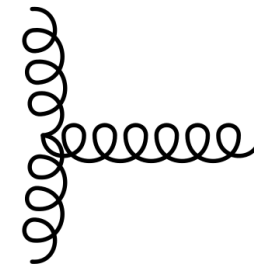
- EXPONENTIATION OF LEFTOVER LOGS \Rightarrow
THRESHOLD RESUMMATION OF $\alpha_s \ln^2(1-x)$, $x = \frac{M^2}{s}$
- LOGS COME IN PAIRS: **SOFT+COLLINEAR** $\rightarrow \ln p_t$ WHEN INTEGRAL OVER p_t NOT PERFORMED \Rightarrow
TRANSVERSE MOMENTUM RESUMMATION OF $\alpha_s \ln^2 \frac{q_T^2}{M^2}$
- IN GLUON CHANNEL **SYMMETRY OF THE TRIPLE GLUON VERTEX** \rightarrow **LARGE LOGS** ALSO WHEN THE **EXCHANGED GLUON** IS SOFT: NO COLLINEAR CONTRIBUTION, **SINGLE LOGS** $\rightarrow \ln \frac{s}{Q^2} \Rightarrow$
HIGH ENERGY RESUMMATION OF $\alpha_s \ln \frac{1}{x}$

GLUON RADIATION

$$\sigma(\tau, M^2) = \int_y^1 \frac{dy}{y} P\left(\frac{x}{y}\right) \int_{\mu^2}^{(s-M^2)^2/s} \frac{dk_t^2}{k_t^2} \hat{\sigma}(y, M^2)$$

THE GLUON SPLITTING FUNCTION:

$$P_{gg}(x) = 2C_A \left[\frac{x}{(1-x)_+} + \frac{1-x}{x} + x(1-x) \right] + \beta_0 \delta(1-x)$$



LOGARITHMICALLY ENHANCED TERMS

- **INFRARED LOGS:** $\int_{\tau}^1 dy \frac{1}{1-y}_+ \sim \ln(1-\tau)$
- **UV LOGS:** $\int_{\tau}^1 dy \frac{1}{y} \sim \ln(\tau)$
- **COLLINEAR LOGS:** $\int_{\mu^2}^{(s-M^2)^2/s} \frac{dk_t^2}{k_t^2} \sim \ln \left[\frac{Q^2}{\mu^2} \frac{(1-\tau)^2}{\tau} \right] = \ln \frac{Q^2}{\mu^2} + \ln(1-\tau)^2 + \ln \tau$

RESUMMATION: A TIMELINE



EARLY

- Balitski, Fadin, Kuraev, Lipatov, 1976-1978 STRUCTURE OF HIGH-ENERGY LOGS
- Dokshitzer, Dyakonov, Troyan, 1979 STRUCTURE OF p_T LOGS
- Parisi, Petronzio, 1979 LL TRANSVERSE MOMENTUM RESUMMATION
- Parisi, 1980; Curci, Greco, 1980 LL SOFT GLUON RESUMMATION
- Jaroszewicz, 1980 LL HIGH ENERGY RES. OF ANOMALOUS DIMENSIONS



CLASSIC

- Collins, Soper, Sterman, 1984 TRANSVERSE MOMENTUM: GENERAL STRUCTURE & ARGUMENT AND NLL RESULT (DRELL-YAN)
- Sterman, 1987: THRESHOLD: GENERAL STRUCTURE & ARGUMENT
- Catani, Trentadue, 1989 SOFT GLUON: NLL RESULT (DY, DIS)
- Catani, Ciafaloni, Hautmann, 1990 HIGH ENERGY: GENERAL FORMALISM FOR PURE GLUE
- Catani, Hautmann, 1993 HIGH ENERGY: GENERAL FORMALISM INCLUDING QUARKS



15th-17th July 2013

THE STRUCTURE OF RESUMMED EXPRESSIONS THRESHOLD RESUMMATION

LOG COUNTING

$$C_{\text{res}}(N, \alpha_s) = g_0(\alpha_s) \exp \left[\frac{1}{\alpha_s} g_1(\alpha_s \ln N) + g_2(\alpha_s \ln N) + \alpha_s g_3(\alpha_s \ln N) + \dots \right];$$

$$g_0(\alpha_s) = 1 + \alpha_s g_{0,1} + \alpha_s^2 g_{0,2} + \mathcal{O}(\alpha_s^3); \quad g_1(\lambda) = \sum_{k=2}^{\infty} g_{1,k} \lambda^k, \quad g_i(\lambda) = \sum_{k=1}^{\infty} g_{i,k} \lambda^k \quad \text{FOR } i \geq 2$$

LOG APPROX.	XSECT ACCURACY	EXP. ACCURACY: $\alpha_s^n L^k$	g_0 ACCURACY: α_s^i
LL	$k = 2n$	$k = n + 1$	0
NLL	$2n - 2 \leq k \leq 2n$	$k = n$	1
NNLL	$2n - 4 \leq k \leq 2n$	$k = n - 1$	2

THE RESUMMED EXPONENT

$$S \left(M^2, \frac{M^2}{N^2} \right) = \int_{M^2}^{M^2/N^2} \frac{d\mu^2}{\mu^2} \bar{\gamma} \left(\alpha_s(\mu^2), \frac{M^2}{N^2 \mu^2} \right)$$

$$= \int_{M^2}^{M^2/N^2} \frac{d\mu^2}{\mu^2} \left[-A(\alpha_s(\mu^2)) \ln \left(\frac{M^2/N^2}{\mu^2} \right) + B[\alpha_s(\mu^2)] \right].$$

- A, B ARE POWER SERIES IN α_s
- A IS UNIVERSAL, COEFFICIENT OF $\ln N$ IN (DIAGONAL QUARK OR GLUON) ANOMALOUS DIMENSION AT EACH ORDER
- B CONTAINS PROCESS-DEPENDENT TERMS, STARTS AT NLL



15th-17th July 2013

THE STRUCTURE OF RESUMMED EXPRESSIONS

P_t RESUMMATION

THE CROSS SECTION

- PARTONIC DIFFERENTIAL p_T DISTRIBUTION: $\Sigma = \sum_n \alpha_s^n(M^2) \Sigma^{(n)}(p_T, M^2)$;

$$\Sigma^{(n)}(p_T, M^2) = \left[\frac{P_n(\ln(p_T^2/M^2))}{p_T^2/M^2} \right]_+ + Q_n(p_T^2/M^2) + D_n \delta(p_T^2/M^2)$$
- **DIVERGES** AS $p_T \rightarrow 0$ TO ANY FINITE ORDER

RESUMMATION

- PHASE-SPACE FACTORIZATION: LONGITUDINAL \leftrightarrow MELLIN; **TRANSVERSE** \leftrightarrow **FOURIER**
- $\Sigma(\alpha_s, p_t^2/M^2) = \frac{M^2}{2\pi} \int d^2b e^{-i\vec{p}_T \cdot \vec{b}} \Sigma(\alpha_s, \alpha_s L) = \int_0^{+\infty} db b J_0(bq_T) \Sigma(\alpha_s, \alpha_s L)$;
 $\alpha_s = \alpha_s(M^2)$; $L \equiv -\ln b^2 M^2$
- EXPONENTIATION: $\Sigma(\alpha_s, \alpha_s L) = \exp S(\alpha_s, \alpha_s L)$

THE RESUMMED EXPONENT

$$S(\alpha_s, \alpha_s L) \equiv - \int_{\frac{1}{b^2}}^{Q^2} \frac{d\mu^2}{\mu^2} \left[\ln \frac{Q^2}{\mu^2} A(\alpha_s(\mu^2)) + B(\alpha_s(\mu^2)) \right],$$

$$\Rightarrow \Sigma(\alpha_s, \alpha_s L) = H(\alpha_s) \exp \left[Lg^{(1)}(\alpha_s L) + g^{(2)}(\alpha_s L) + \dots \right]$$

- A, B ARE POWER SERIES IN α_s
- A CONTAINS **SOFT** CONTRIBUTIONS, B **PURELY COLLINEAR** (FLAVOR-CONSERVING) CONTRIBUTIONS
- RESUMMATION SET UP SO THAT A AND B ARE **PROCESS-INDEPENDENT** (ONLY DEPEND ON QUARK VS GLUON) (Catani, de Florian, Grazzini, 2000)

RESUMMATION TIMELINE II



MODERN

- Catani, Mangano, Nason, Trentadue, 1996 **SOFT RESUMMATION FORMALISM FOR HADRONIC PROCESSES**
- Contopanagos, Laenen, Sterman, 1997 **GENERAL RG ARGUMENT FOR SUDAKOV RESUMMATION**
- Altarelli, Ball, SF, 2001 **HIGH ENERGY RESUMMATION IN DGLAP EQUATION**

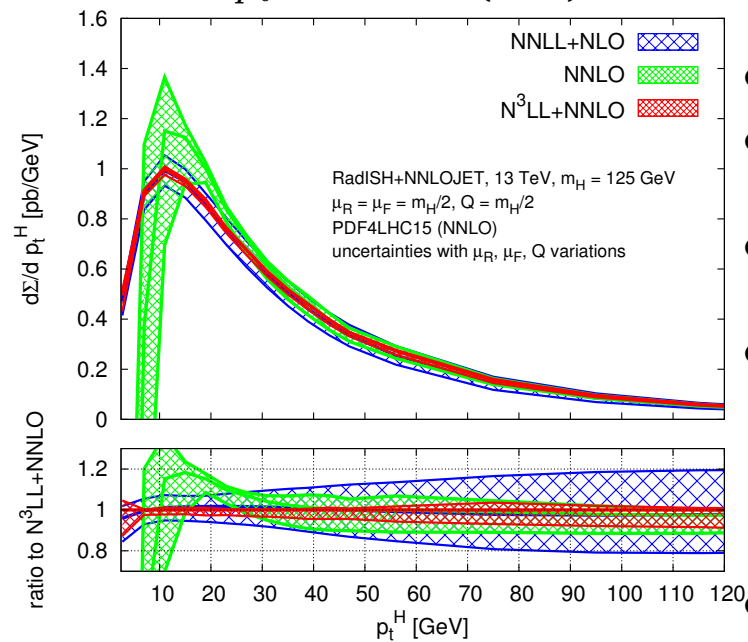


CONTEMPORARY

- Catani, de Florian, Grazzini, 2001 **TRANSVERSE MOMENTUM RESUMMATION UNIVERSALITY & FORMALISM FOR HADRONIC PROCESSES**
- Manohar, 2003 **SCET APPROACH TO THRESHOLD RESUMMATION**
- Ciafaloni, Colferai, Salam, Stasto, 2004 **FULL HIGH ENERGY RESUMMATION OF SPLITTING FUNCTIONS (PURE GLUE)**
- Altarelli, Ball, SF, 2008 **HIGH ENERGY RESUMMATION FOR PHYSICAL PROCESSES**

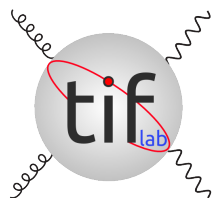
RESUMMATION NOW

HIGGS p_t SPECTRUM (EFT)



(Bizon, Chen,
 Gehrmann-De Ridder, Gehrmann,
 Glover, Huss, Monni, Re,
 Rottoli, Torrielli, 2018)

- SCET vs. DQCD NOT AN ISSUE
- THRESHOLD RESUMMATION
 ⇒ IMPROVE FIXED ORDER
- MATCHING OF p_t RESUMMATION TO FIXED ORDER
 STANDARD FOR p_T SPECTRA
- IMPLEMENTED IN SEVERAL PUBLIC CODES: E.G.
 xFitter/APFEL (Bertone, 2016-2017), TROLL, HELL
 (Bonvini, 2016-2018), TOP++ (Czakon, Mitov, 2016-2018),
 iHixs (Anastasiou, Bühler, Dulat, Herzog, Lazopoulos,
 Mistlberger 2012-2018), ...
- PROGRESS
 - HIGHER ORDERS, MORE PROCESSES
 - COMBINED, CONSISTENT & MORE EXCLUSIVE



SIX GREAT IDEAS ABOUT RESUMMATION

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MOMENTUM-SPACE RESUMMATION

MELLIN/FOURIER

THE PROBLEM:

- **RG** ARGUMENT FOR RESUMMATION NATURALLY FORMULATED IN **FOURIER-MELLIN**:
 - MELLIN \Rightarrow **LONGITUDINAL MOMENTUM CONSERVATION** (UNDOES CONVOLUTION)
 - FOURIER \Rightarrow **TRANSVERSE MOMENTUM CONSERVATION** (FACTORIZES k_t DELTA)
- **EIKONAL EMISSION FACTORIZES** \Rightarrow CAN RESUM (BOTH SOFT & p_t) IN **MOMENTUM SPACE**

- **SCHEMATIC BEHAVIOUR** (FIXED COUPLING)

$$K^{\text{res}} \sim \frac{d}{dp_t} \exp - \left[\alpha_s \ln^2 Q^2 / p_t^2 F \left(\alpha, \ln \frac{Q^2}{p_t^2} \right) \right]$$

\Rightarrow **ZERO RADIUS OF CONVERGENCE!** (DIVERGES FASTER THAN ANY POWER OF LOG)

- **EXPANSION** AT **LL, NLL...** LEADS TO **CONVERGENT** RESULT,

FINITE RADIUS OF CONVERGENCE: $K^{\text{res}} \sim \frac{d}{dp_t} \exp - [\alpha_s \ln^2 Q^2 / p_t^2] \frac{\Gamma \left(1 - 2\alpha_s \ln \frac{Q^2}{p_t^2} \right)}{\Gamma \left(1 + 2\alpha_s \ln \frac{Q^2}{p_t^2} \right)}$

\Rightarrow **BAD PERTURBATIVE EXPANSION**

MOMENTUM SPACE A SOLUTION

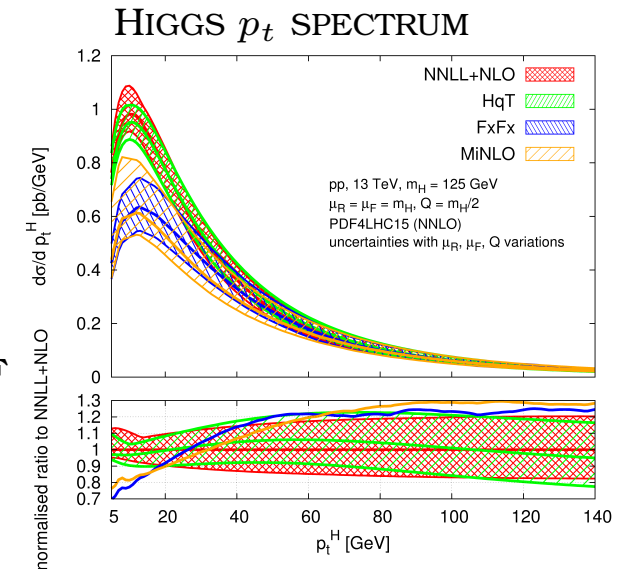
(Monni, Re, Torrielli, 2016; also Ebert, Tackmann, 2017)

DIVERGENCE & SINGULARITIES WHEN **EXPONENTIATING** INDEPENDENT SMALL p_t EMISSION
DUE TO **THE NEGLECT OF CONFIGURATIONS** WHERE p_t **SMALL DUE TO CANCELLATIONS**
 \Rightarrow DOMINANT AS $p_t \rightarrow 0$ (Parisi, Petronzio, 1979)

- CONSTRUCT **CUMULATIVE CROSS-SECTION**

$$\Sigma(p_t) = \int_0^{p_t} dp'_t \frac{d\sigma(p'_t)}{dp'_t}$$

- **DIVERGENT** \Leftrightarrow **EXPANDING** EMISSIONS k_t^i ABOUT p_t
- **ORDER** EMISSIONS IN k_t , **EXPAND ABOUT LARGEST** k_T^1
- CAN **DEFINE ITERATIVELY** n -EMISSION CUMULANT IN TERMS OF $n - 1$
- CAN **PROVE EQUIVALENCE** TO STANDARD FORMALISM UP TO SUBLEADING CORRECTIONS;
SINGULAR TERMS SHIFTED TO HIGHER ORDERS

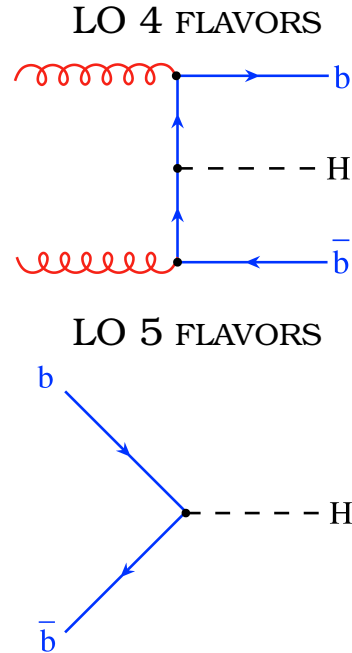


(Monni, Re, Torrielli, 2016)

MASSIVE EVOLUTION

AN OLD PROBLEM: MASSIVE QUARK SCHEMES

EXAMPLE: $b\bar{b} \rightarrow H$

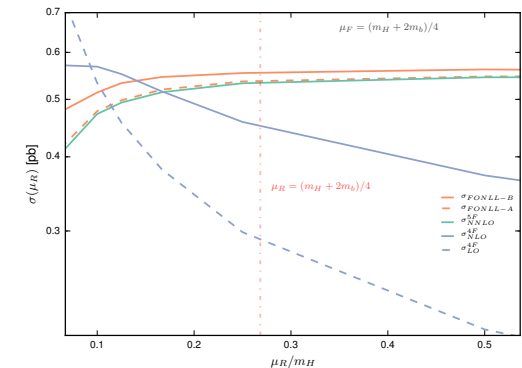


- **4FS** \Rightarrow **MASSIVE** B, NO b IN DGLAP EVOLUTION AND β FUNCTION
- **5FS** \Rightarrow m_b IN DGLAP EVOLUTION AND β FUNCTION BUT b **MASS NEGLECTED**

CLASSIC SOLUTION: MATCHED SCHEMES

- COLLINEAR FACTORIZATION ALSO HOLDS FOR MASSIVE QUARKS (Collins, 1998)
- RE-EXPRESS 4FS IN TERMS OF 5FS (OR VICE-VERSA)
- COMBINE & SUBTRACT DOUBLE COUNTING
- $b\bar{b}H$: PERTURBATIVE INSTABILITY OF 4FS REMOVED BY RESUMMATION
- MASS CORRECTIONS
NEEDED FOR PERCENTAGE ACCURACY, EVEN FOR TOTAL XSECTS

4FS, 5FS VS MATCHED (FONLL) RENORM. SCALE DEP.



WHAT'S THE PROBLEM?

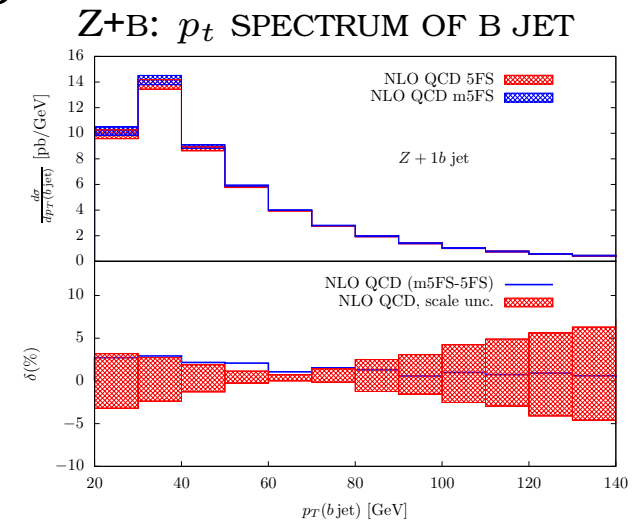
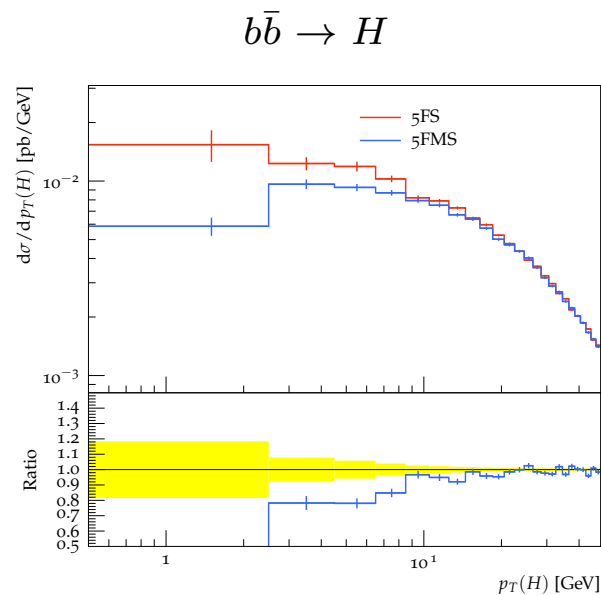
- **CUMBERSOME**, ESPECIALLY FOR DIFFERENTIAL OBSERVABLES
- **NOT EASY TO IMPLEMENT/INTERFACE** IN MONTECARLOS

SOLUTION: MASSIVE 5FS

((Krauss, Napoletano, 2018))

- **MASSIVE SPLITTING FUNCTION**
- **SUBSET** OF UNIVERSAL INITIAL-STATE MASS CORRECTIONS **RESUMMED**
- SUBSET OF MATCHED SCHEME CAPTURED, BUT RESUMMED TO ALL ORDERS

5FS vs MFS



(Figuroa, Honeywell, Quackenbusch, Reina, Reuschle, Wackerath, 2018)

MIXED QCD-EW EVOLUTION

THE PROBLEM OF EW SUDAKOVs

- **KLN** CANCELLATION OF IR SINGULARITIES HOLDS IN **QED**
- IN **NONABELIAN** CASE, **CANCELLATION** ONLY FOR GAUGE GROUP **SINGLET**
- **PROTON** IS NOT EW SINGLET \Rightarrow **IR MASS SINGULARITIES DO NOT CANCEL** BETWEEN REAL AND VIRTUAL
- **EXPLICIT MASS DEPENDENCE IN VIRTUAL CORRECTION**,
REAL CONTRIBUTION HAS NO $+$ PRESCRIPTION
 \Rightarrow SINGULAR SPLITTING FUNCTIONS (M. Ciafaloni, P. Ciafaloni, Comelli, 2000-2005):

$$P_V \sim \delta(1-x) \ln \frac{Q^2}{k_t^2 \max},$$

$$P^R \sim \frac{1}{1-x};$$

$$\frac{d}{d \ln Q^2} F(x, Q^2) = \int_x^{y^{\max}} P f\left(\frac{y}{x}, Q^2\right); \quad P = P^V + P^R$$

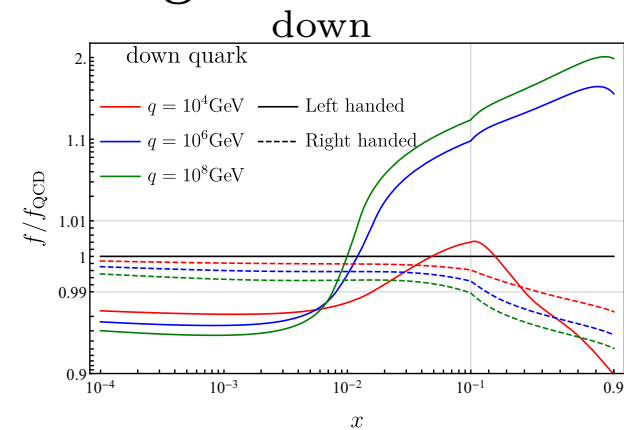
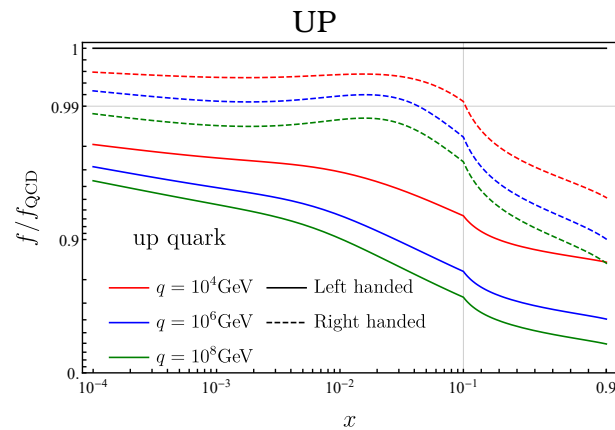
- **DOUBLE LOGS** $\alpha_{EW} \ln^2 \frac{Q^2}{M_W^2}$ **TO ALL ORDERS**

A PRACTICAL SOLUTION SOLVING SM EVOLUTION EQUATIONS

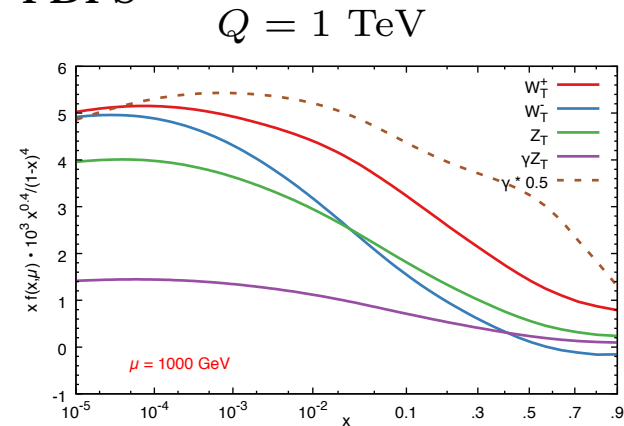
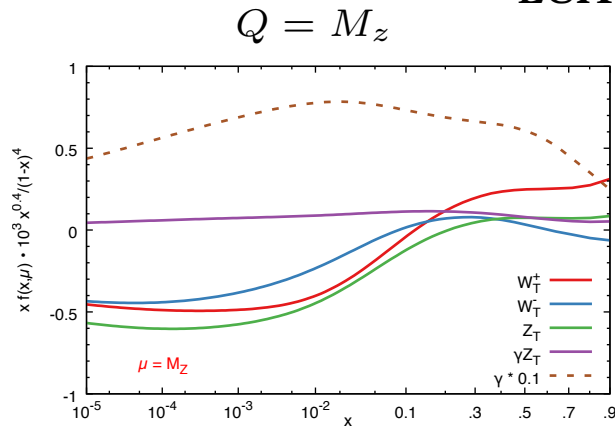
(Bauer, Ferland, Webber, 2017)

- SOLVE EVOLUTION EQUATIONS IN THE FULL STANDARD MODEL
- MATCH RESULTS TO FIXED ORDER CALCULATIONS
- INITIAL GAUGE BOSON PDF CAN BE DETERMINED BY THE LUX METHOD (Fornal, Manohar, Waalewijn, 2019)

FULL SM PDF EVOLUTION: RATIO TO QCD



“LUX” TRANSVERSE W PDFs



NEXT-TO LEADING POWER

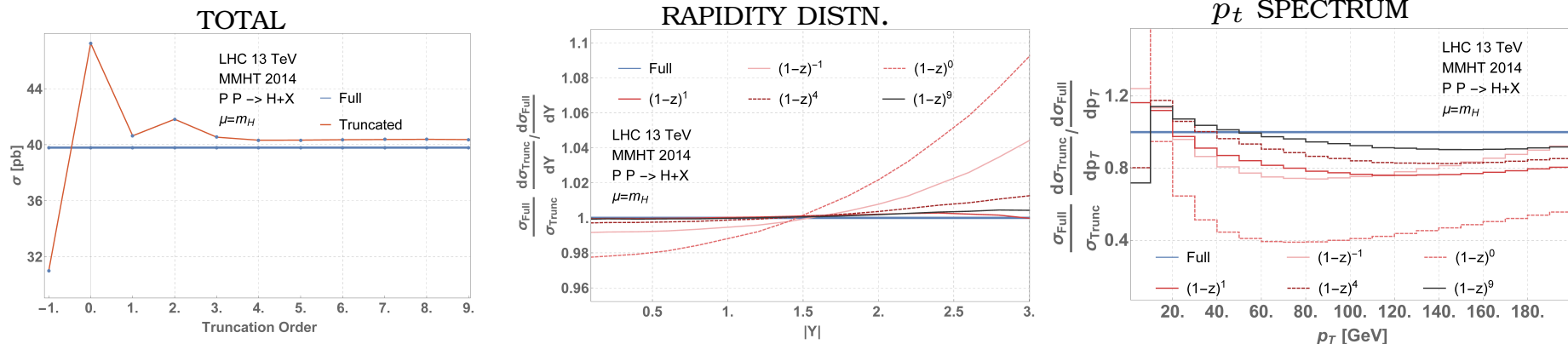
SOFT EXPANSION(S)

- BOTH IN THRESHOLD AND HE LIMIT: RESUMMATION \Rightarrow
 - IMPROVEMENT OF FIXED ORDER
 - APPROXIMATE HIGHER ORDER (HQ MASS DEP, MULTISCALE)
- NEXT-TO-LEADING POWER LOGARITHMICALLY ENHANCED:

$$C^{(n)}(x) \underset{x \rightarrow 1}{=} \alpha_s^n \frac{\ln^{2n-1}(1-x)}{1-x_+} + \delta(1-x) + \ln^{2n}(1-x) + \dots$$
- LL, NLP RESUMMATION \Leftrightarrow DGLAP SPLITTING FUNCTION EXPANDED TO NLP
- NLP GOOD APPROX, ESPECIALLY IF RESCALED

NNLO HIGGS IN GLUON FUSION: SOFT EXPANSION

(Dulat, Mistlberger, Pelloni, 2018)



NLP PROGRESS

- **METHOD OF REGIONS** (Laenen et al, 2013....)
 - SEPARATE INTEGRATION REGIONS OVER MOMENTA THROUGH SCALING
 - COMBINE WITH FACTORIZATION \Rightarrow CLASSIFY EMISSION FROM INTERNAL BLOBS DRESSED WITH RADIATION FROM EXTERNAL LINES
- RAPID **RECENT PROGRESS** BOTH USING DQCD & SCET, BOTH IN HE & SOFT LIMIT

NLO NLP UNIVERSALITY

(Del Duca, Laenen, Magnea, Vernazza, White, 2018)

- **NEXT-TO-SOFT THEOREM** (E. Casali, 2014; Bonocore et al, 2015)
 \Leftrightarrow EIKONAL-LIKE **NLP EMISSION FORMULA**
- EFFECTIVELY, **NLP** OBTAINED FROM **SHIFT IN BORN KINEMATICS**:
 Born: $p_1 + p_2 \rightarrow X$; NLP NLO $p_1 \rightarrow p_1 - \frac{1}{2} \left(p_1 \frac{p_2 \cdot k}{p_1 \cdot p_2} - p_2 \frac{p_2 \cdot k}{p_1 \cdot p_2} + k \right)$, & SIMILAR FOR p_2
- **NLP NLO**: $C(x) = K(x, \varepsilon) C^{\text{Born}}(x_s)$;

$$K(x, \varepsilon) = \left(\frac{\mu^2}{s} \right)^\varepsilon \left[\frac{2-2D_0(x)}{\varepsilon} + 4D_1(x) - 4 \ln(1-x) \right];$$

$$D_n(x) = \left(\frac{\ln^n(1-x)}{1-x} \right)_+$$
- **HIGGS IN GLUON FUSION**:
 - ALL **NLO LOG DEPENDENCE** COMES FROM **UNIVERSAL NLP FACTOR** $K(x, \varepsilon)$
 - FULL m_t **DEPENDENCE** INCLUDED THROUGH **BORN FUNCTION** $F(x\tau, \varepsilon)$, $\tau = \frac{m_H^2}{s}$,

$$F(\tau, \varepsilon) = \frac{9}{4} \frac{1}{\tau^2} \left| 1 + \left(1 - \frac{1}{\tau} \right) \arcsin^2(\sqrt{\tau}) \right|^2 + O(\varepsilon)$$

DIVERGENT OBSERVABLES

RESUMMING DIVERGENCES

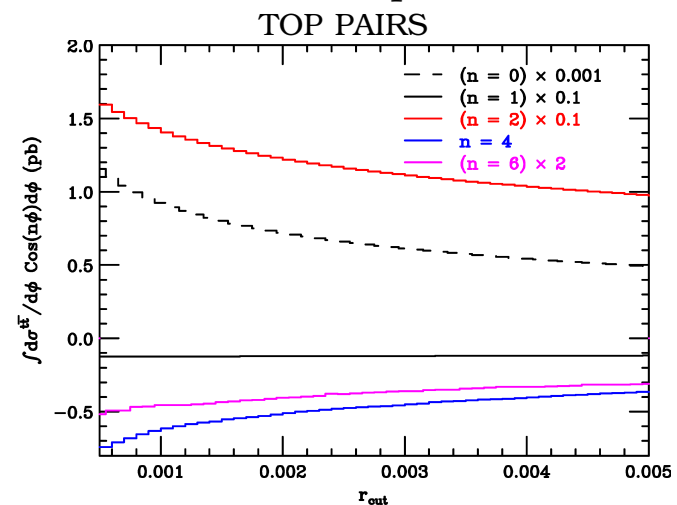
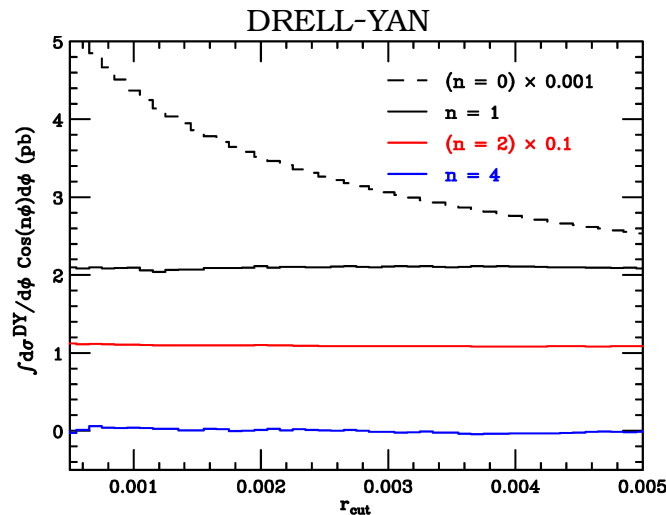
- **DIVERGENCES AT KINEMATIC BOUNDARIES** ROUTINELY REMOVED BY RESUMMATION
- **IRC SAFE BUT DIVERGENT** OBSERVABLES MADE **FINITE** BY RESUMMATION

AZIMUTHAL VARIABLES

(Catani, Grazzini, Sargsyan, 2017)

- $h(p_1)h(p_2) \rightarrow F(p_3, p_4) + X \Rightarrow$ DY INTO DILEPTONS, TOP PAIRS, ...
- FINAL-STATE KINEMATICS M, p_T, y OF F ; θ, ϕ OF p_3 IN COLLINS-SOPER FRAME (REST FRAME OF F)
- $\frac{d\sigma}{d\phi dp_t} \Rightarrow$ **NONINTEGRABLE SINGULARITY** AS $p_t \rightarrow 0 \Rightarrow \frac{d\sigma}{d\phi}$ **DIVERGENT** IF EITHER
 - **INITIAL STATE GLUON** (SOMETIMES)
 - **COLORS FINAL STATE** (ALWAYS)

AZIMUTHAL ANGULAR HARMONICS INTEGRATED DOWN TO $p_t = r_{\text{cut}}$

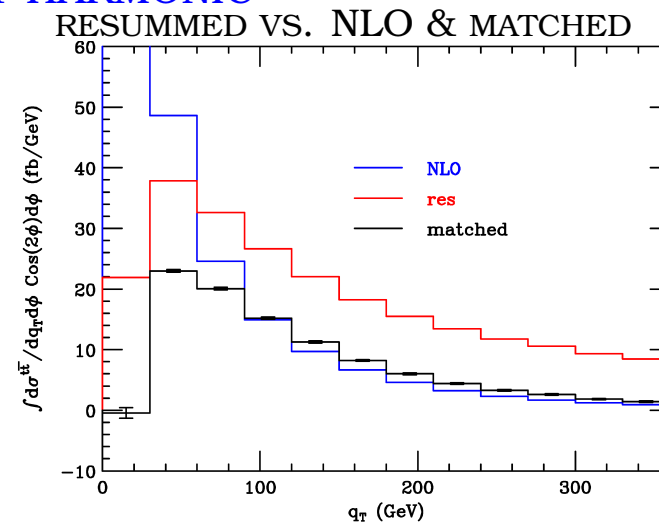
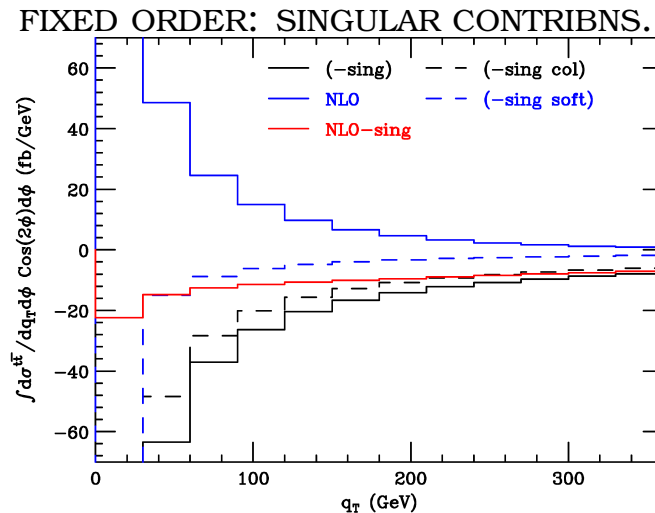


RESUMMING DIVERGENCES

(Catani, Grazzini, Sargsyan, 2017)

- **DIVERGENCE** DUE TO **MISMATCH** BETWEEN **VIRTUAL** & **REAL** AT FIXED ORDER
- **VIRTUAL CANNOT LEAD TO AZIMUTHAL CORRELATION** \Rightarrow **CANNOT CANCEL**
 - **SINGULAR REAL** CONTRIBUTIONS DUE TO COLLINEAR SPIN-CORRELATIONS (INITIAL-STATE GLUONS)
 - **LARGE-ANGLE RADIATION** FROM FINAL-STATE PARTICLES (FINAL-STATE COLORED STATES)
- **RESUMMATION** REMOVES THE DIVERGENCE THROUGH **SUDAKOV SUPPRESSION**

TOP PRODUCTION: FIRST HARMONIC



RESUMMED PDFs

WHAT ABOUT PDFs?

$$\Delta_N(Q^2) = \frac{W_N(Q^2)}{[F_N(Q^2)]^2},$$

(Catani, Trentadue, 1987)

- RATIO OF PHYSICAL PROCESSES \Rightarrow RESUMMATION
- THE PDF IS THE DENOMINATOR
- BUT NOT RESUMMED IN AVAILABLE PDF SETS
- KEPT UNDER CONTROL WITH CUTS

PDFs WITH THRESHOLD RESUMMATION

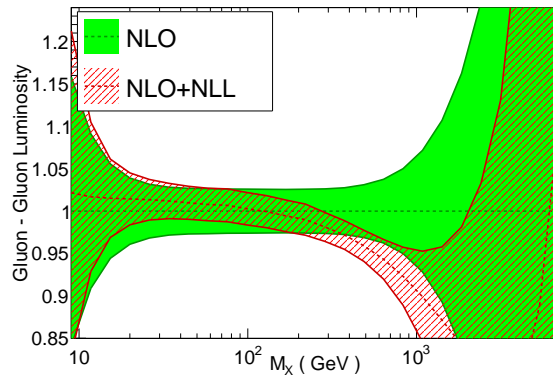
EFFECTS ARE SMALL

- FIRST SET: NNPDF3.0resum
- EFFECT ON PDFs **COMPARABLE TO** EFFECT ON **MATRIX ELEMENT, ANTICORRELATED TO IT**
- **RESUMMATION INCLUDED** IN FIT (DIS, DY, TOP DATA), EFFECTS **VISIBLE AT NLO, LARGE x**
- **PERHAPS RELEVANT FOR NEW PHYSICS SEARCHES**

(Bonvini et al., 2015)

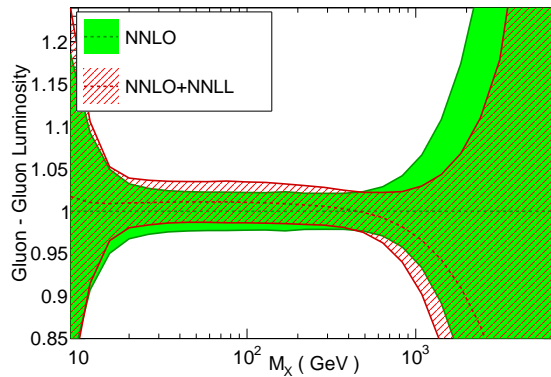
GLUON: NLO vs NLL

LHC 13 TeV, NNPDF3.0 DIS+DY+Top, $\alpha_s(M_Z)=0.118$



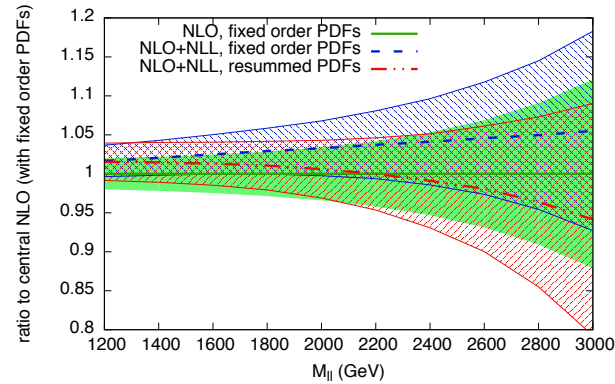
GLUON: NNLO vs NNLL

LHC 13 TeV, NNPDF3.0 DIS+DY+Top, $\alpha_s(M_Z)=0.118$



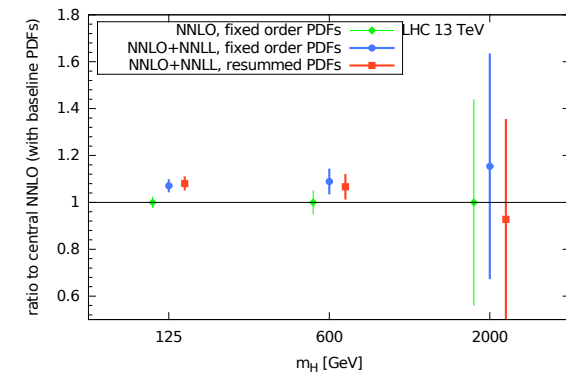
SLEPTON PAIR PRODUCTION

Slepton pair invariant mass, pp @ 13 TeV, $m_l = 564$ GeV.



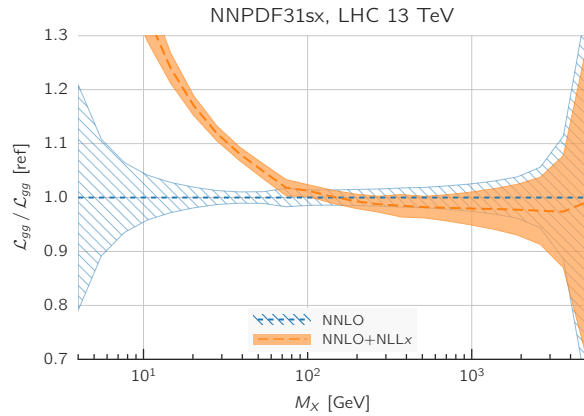
HIGGS IN GLUON FUSION VS m_H

Higgs cross section: gluon fusion



PDFs WITH HIGH ENERGY RESUMMATION

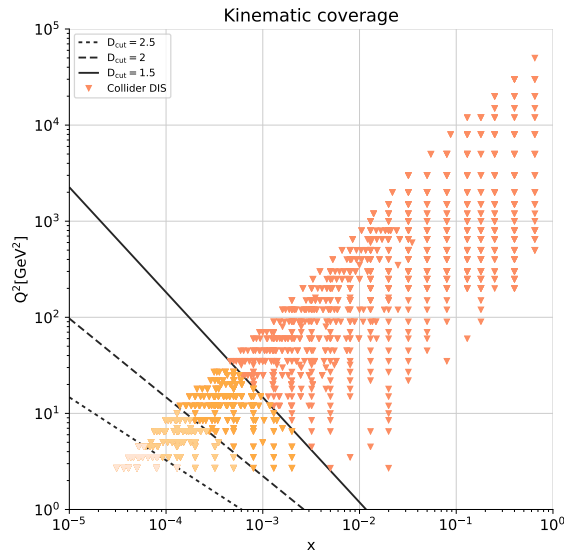
GLUON LUMINOSITY



- FIRST SET: NNPDF3.0sx
- HIGH ENERGY RESUMMATION INCLUDED IN GLAP EVOLUTION & FOR DIS COEFFICIENT FUNCTIONS
- STABILIZES PERTURBATIVE EXPANSION
- VISIBLE EFFECTS FOR LIGHT FINAL STATES (b PRODUCTION AT LHC) & FOR FUTURE COLLIDERS

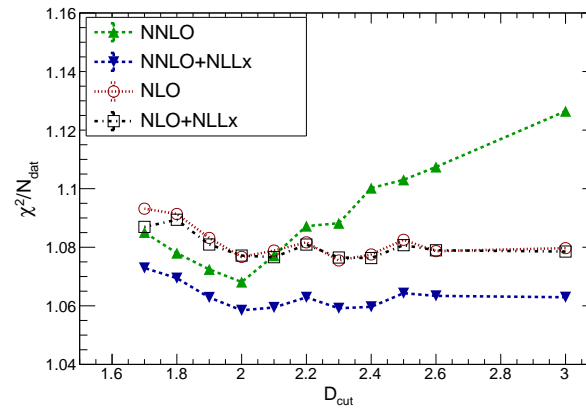
(Ball et al., 2017)

KINEMATIC CUTS



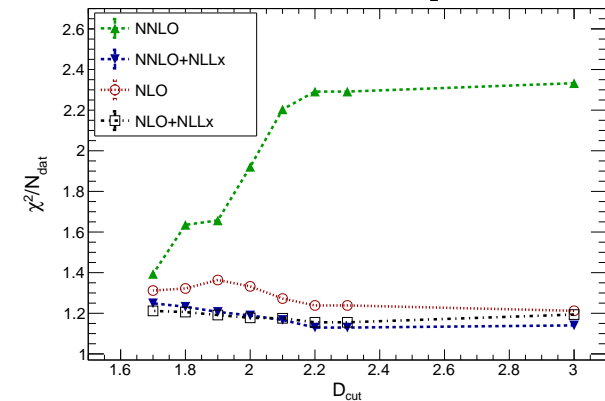
INCLUSIVE F_2 FIT QUALITY

NNPDF3.1sx, HERA NC inclusive data



CHARM F_2^c FIT QUALITY

NNPDF3.1sx, HERA F_2^c data



AN OUTLOOK?

A RESUMMATION WISHLIST

- **CONSISTENT, FULLY EXCLUSIVE SOFT RESUMMATION**
(GGHIGGS, DRELL-YAN, TOP, INCLUSIVE JETS):
DIFFERENTIAL IN p_T , RAPIDITY, ALWAYS THRESHOLD-RESUMMED UPON INTEGRATION
- **NEXT-TO-LEADING LOG HIGH-ENERGY FACTORIZATION AND RESUMMATION**
FOR HADRONIC PROCESSES (GLUON-INDUCED: HIGGS, HEAVY QUARKS)
- **MULTISCALE RESUMMATION WITH HEAVY QUARKS**
(GGHIGGS p_t SPECTRUM $\ln \frac{m_b}{p_t}$)
- **THE LIMITS OF FACTORIZATION: WHEN DOES IT BREAK DOWN?**
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