

NLO EW Corrections for W^+Z scattering at the LHC

$pp \rightarrow e^+ \nu_e \mu^+ \mu^- jj + X @ \mathcal{O}(\alpha^6)$ and $\mathcal{O}(\alpha^7)$ for $\sqrt{s} = 13$ TeV

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with:

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- What is vector-boson scattering?
- Experimental status
- Discriminating between QCD and EW production

2 NLO EW corrections

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- Acknowledgments

Vector-boson scattering in a nutshell

→ Scattering of two (massive) vector-bosons, e.g.:

- $W^\pm W^\pm \rightarrow W^\pm W^\pm$ ("like-sign W scattering")
- $W^\pm Z \rightarrow W^\pm Z$

$$W^+ Z \rightarrow W^+ Z$$

$$\mathcal{M}_{\text{VBS}} = \begin{array}{c} \text{Feynman diagram 1} \\ + \\ \text{Feynman diagram 2} \\ + \\ \text{Feynman diagram 3} \\ + \\ \text{Feynman diagram 4} \end{array}$$

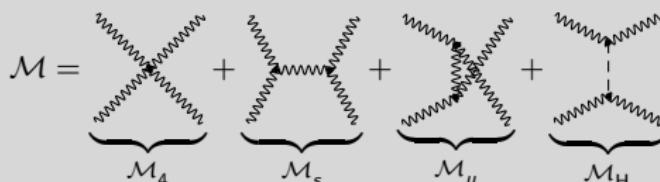
$$pp \rightarrow e^+ \nu_e \mu^+ \mu^- jj + X$$

$$\mathcal{M}_{\text{VBS@LHC}} = \begin{array}{c} \text{Feynman diagram 1} \\ + \\ \text{Feynman diagram 2} \\ + \dots \end{array}$$

Vector-boson scattering (VBS) physics program:

- Constrain anomalous quartic gauge couplings (with triple-gauge boson prod.)
- Measure Higgs-vector-vector couplings, complementary to on-shell Higgs decay measurements
- Probe EW symmetry breaking: interplay between triple and quartic gauge couplings and the Higgs boson(s); large cancellations for longitudinal VBS: ensures **tree-level unitarity**
- Precise prediction of the SM cross section needed

Longitudinal VBS: Tree-level (non-)unitarity

 $W^+ Z \rightarrow W^+ Z$ @ $M_H = 125 \text{ GeV}$ 

$$\mathcal{M}_4 \propto -s^2 - u^2 - 4su + 2(M_W^2 + M_Z^2) \frac{s^2 + 6su + u^2}{s + u} + \dots$$

$$\mathcal{M}_s \propto s^2 + 2su - 2M_W^2 \frac{3su + u^2}{s + u} - 2M_Z^2 \frac{2u^2 + 3su - s^2}{s + u} - \frac{M_Z^4}{M_W^2} s + \dots$$

$$\mathcal{M}_u \propto u^2 + 2su - 2M_W^2 \frac{3su + s^2}{s + u} - 2M_Z^2 \frac{2s^2 + 3su - u^2}{s + u} - \frac{M_Z^4}{M_W^2} u + \dots$$

$$\mathcal{M}_H \propto -\frac{M_Z^4}{M_W^2} \frac{t^2(t - 4M_W^2)(t - 4M_Z^2)}{(t - M_H)(t - 2M_W^2)(t - 2M_Z^2)} = -\frac{M_Z^4}{M_W^2} t + \dots$$

$$\mathcal{M} = \mathcal{M}_4 + \mathcal{M}_s + \mathcal{M}_u + \mathcal{M}_H \propto 0 + \dots$$

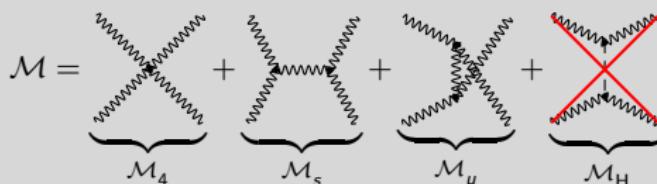
Example from [Schwartz]

Assuming
 $|t| \gg M_H^2, M_Z^2, M_W^2$

Longitudinal VBS: Tree-level (non-)unitarity

$W^+ Z \rightarrow W^+ Z$

@ $M_H = \infty$



$$\mathcal{M}_4 \propto -s^2 - u^2 - 4su + 2(M_W^2 + M_Z^2) \frac{s^2 + 6su + u^2}{s + u} + \dots$$

$$\mathcal{M}_s \propto s^2 + 2su - 2M_W^2 \frac{3su + u^2}{s + u} - 2M_Z^2 \frac{2u^2 + 3su - s^2}{s + u} - \frac{M_Z^4}{M_W^2} s + \dots$$

$$\mathcal{M}_u \propto u^2 + 2su - 2M_W^2 \frac{3su + s^2}{s + u} - 2M_Z^2 \frac{2s^2 + 3su - u^2}{s + u} - \frac{M_Z^4}{M_W^2} u + \dots$$

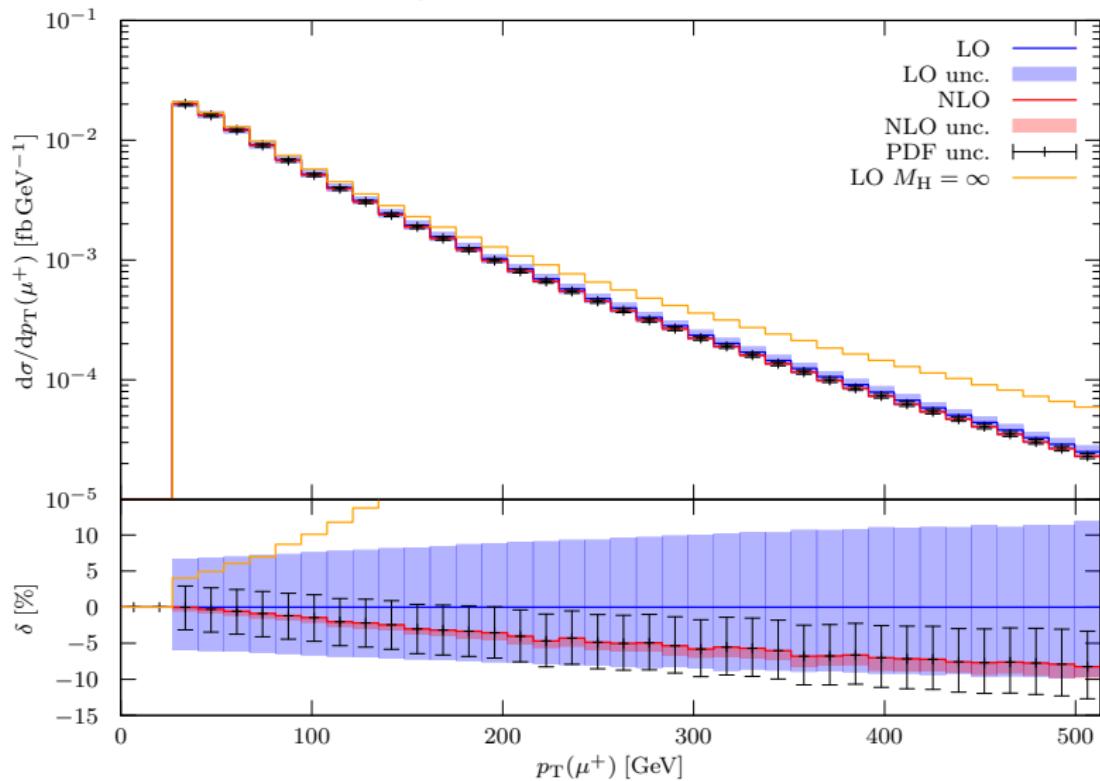
$$\mathcal{M}_H \propto -\frac{M_Z^4}{M_W^2} \frac{t^2(t - 4M_W^2)(t - 4M_Z^2)}{(t - M_H)(t - 2M_W^2)(t - 2M_Z^2)} = 0$$

$$\mathcal{M} = \mathcal{M}_4 + \mathcal{M}_s + \mathcal{M}_u + \mathcal{M}_H \propto -\frac{M_Z^4}{M_W^2} (s + u) + \dots$$

Example from [Schwartz]

→ $M_H = \infty$ estimates the maximal effect of different Higgs couplings

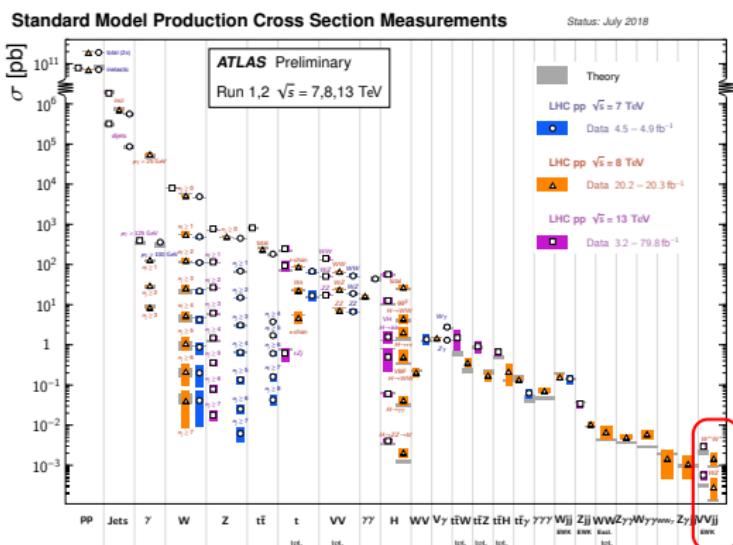
$M_H = \infty$ for $pp \rightarrow e^+ \nu_e \mu^+ \nu_\mu jj + X$



→ Large positive correction, range for extended Higgs sector

Experimental status for VBS, EW $pp \rightarrow e^+ \nu_e \mu^+ \mu^- jj + X$

→ VBS processes are $\mathcal{O}(1\text{fb})$, need large \sqrt{s} and \mathcal{L} :

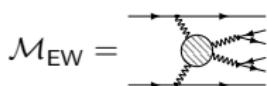


(dinosaur plot from the [\[ATLAS Collaboration\]](#))

- ATLAS 8 TeV: [\[CERN-EP-2016-017\]](#)
- ATLAS 13 TeV: Obsers. with 5.6σ sig. ($\mathcal{L} = 36.1 \text{ fb}^{-1}$)
[\[ATLAS-CONF-2018-033\]](#)
- CMS 13 TeV: Meas. with 1.9σ sig. ($\mathcal{L} = 35.9 \text{ fb}^{-1}$)
[\[CMS-PAS-SMP-18-001\]](#)
- Easiest VBS channel is $W^+W^+ \rightarrow W^+W^+$, full NLO corrections available [\[Biedermann, Denner, Pellen\]](#)
- Next channel: $W^+Z \rightarrow W^+Z$

Discriminating between EW and QCD production

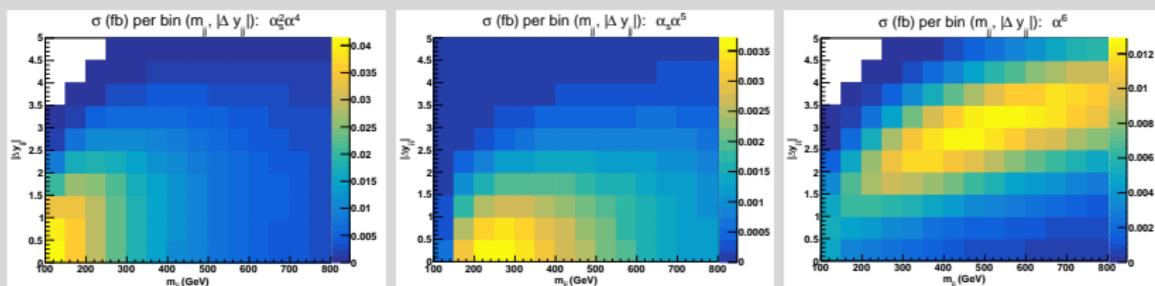
→ At LO, three different coupling orders:



- $\mathcal{O}(\alpha^4 \alpha_s^2)$: $|\mathcal{M}_{\text{QCD}}|^2$
- $\mathcal{O}(\alpha^5 \alpha_s^1)$: $2\Re \left\{ \mathcal{M}_{\text{QCD}}^* \mathcal{M}_{\text{EW}} \right\}$
- $\mathcal{O}(\alpha^6 \alpha_s^0)$: $|\mathcal{M}_{\text{EW}}|^2$

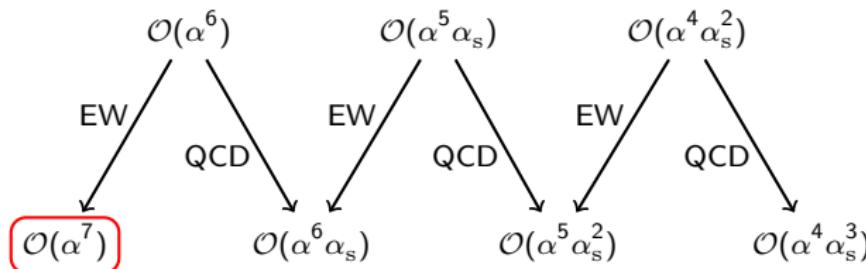
How to maximize the EW production ("signal")?

($\text{pp} \rightarrow e^+ \nu_e \mu^+ \nu_\mu jj + X$)



(plots from VBSCAN WG1 report [Ballestrero, et. al.])

- Observables $M_{j_1 j_2}$ and $\Delta y_{j_1 j_2}$ are used to discriminate the QCD from the EW production
- In the fiducial PS region, EW > QCD for like-sign scattering (no initial-state gluons), for $W^+ Z$ -scattering: QCD > EW

LO and NLO for $pp \rightarrow e^+ \nu_e \mu^+ \mu^- jj + X$ 

- All LOs presented in Sec. V.3 of the SM Les Houches 2017 report [Bendavid et. al.]: QCD (~80%) dominates over EW
- Approx. $\mathcal{O}(\alpha^6 \alpha_s^1)$: [Bozzi, Jäger, Oleari, Zeppenfeld]
- $\mathcal{O}(\alpha^4 \alpha_s^3)$ calculation available [Campanario, Kerner, Ninh, Zeppenfeld]
- $\mathcal{O}(\alpha^7)$ EW corrections desirable, because like-sign case shows large corrections (-16%)

Validation and checks

We performed **two independent calculations** for both $\mathcal{O}(\alpha^6)$ and $\mathcal{O}(\alpha^7)$:

“Freiburg”

“Würzburg”

- MEs from OpenLoops [Cascioli, Maierhöfer, Pozzorini]
 - Loops evaluated with DD (COLI fallback) from COLLIER [Denner, Dittmaier, Hofer]
 - General purpose Monte Carlo [CS]
 - Dipole subtraction [Catani, Seymour] to regularize IR singularities
 - PDFs from LHAPDF 6 [Buckley, et. al.]
- MEs from RECOLA [Actis, Denner, Hofer, Scharf, Uccirati]
 - Loops evaluated with COLI (and DD) from COLLIER
 - MoCaNLO [Feger] used by M. Pellen
 - CS dipole subtraction with α -dependent dipoles [Nagy]
 - PDFs from LHAPDF 6

Extensive checks:

- NLO virtuals checked against each other for 1000 PS points passing the cuts
- Integrated cross sections
- Each bin of 23 differential distributions, ca. 7800 bins

Fiducial phase space volume for $\text{pp} \rightarrow e^+ \nu_e \mu^+ \mu^- jj + X$

Cuts chosen similar to the ATLAS

8 TeV-analysis [CERN-EP-2016-017]:

- At least two $R = 0.4$ anti- k_t jets with $p_T > 30 \text{ GeV}$, $|\eta| < 4.5$, and $\Delta R_{j\ell} > 0.3$
- $M_{j_1 j_2} > 500 \text{ GeV}$, no $\Delta\eta_{j_1 j_2}$ cut¹
- $p_{T,\ell} > 20 \text{ GeV}$ and $|y_\ell| < 2.5$
- $p_{T,\text{miss}} > 30 \text{ GeV}$
- $|M_{\mu\bar{\mu}} - M_Z| < 10 \text{ GeV}$
- $\Delta R_{\ell\ell} > 0.3$

Other:

- Photons recombined with charged particles using anti- k_t algorithm with $R = 0.1$
- PDFs: NNPDF30_nlo_as_0118_qed
- $\sqrt{s} = 13 \text{ TeV}$

Complex mass scheme [Denner, Dittmaier, Roth, Wackerroth][Denner, Dittmaier, Roth, Wieders], input parameters:

- $G_\mu = 1.663\,787 \times 10^{-5} \text{ GeV}^{-2}$
- $M_W = 80.357\,97 \text{ GeV}$, $\Gamma_W = 2.084\,30 \text{ GeV}$
- $M_Z = 91.153\,48 \text{ GeV}$, $\Gamma_Z = 2.494\,27 \text{ GeV}$
- $M_H = 125.0 \text{ GeV}$, $\Gamma_H = 4.07 \times 10^{-3} \text{ GeV}$

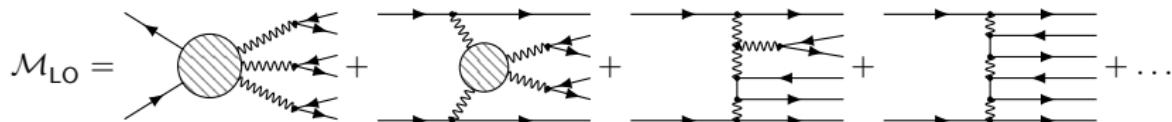
with coupling calculated as:

$$\alpha = \frac{\sqrt{2}}{\pi} G_\mu M_W^2 \left(1 - \frac{M_W^2}{M_Z^2} \right)$$

Scale choice: $\mu_F = (1/2, 1, 2) \cdot M_W$
→ No dependence on μ_R , since processes do not depend on α_s !

¹Unused in the ATLAS 8 TeV-analysis, but used both in the ATLAS and CMS 13 TeV analyses

Feynman diagrams and partonic channels

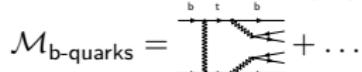


Borns and Born-like:

- $uu \rightarrow e^+ \nu_e \mu^+ \mu^- du$ (~47% XS),
- $du \rightarrow e^+ \nu_e \mu^+ \mu^- dd$ (~18% XS),
- ... + 38 more: **bottleneck are virtuals**

Not included, small or negligible:

- $\gamma\gamma \rightarrow e^+ \nu_e \mu^+ \mu^- (d\bar{u}/s\bar{c})$, and
- $bu \rightarrow e^+ \nu_e \mu^+ \mu^- db$,
- ... + 7 more, with resonant top-quarks:



Reals:

- $uu \rightarrow e^+ \nu_e \mu^+ \mu^- du\gamma$,
- $du \rightarrow e^+ \nu_e \mu^+ \mu^- dd\gamma$,
- ... + 38 more,

Reals not yet calculated, expected to be small:

- $\gamma u \rightarrow e^+ \nu_e \mu^+ \mu^- du\bar{u}$,
- ... + 27 more,
- $\gamma\gamma \rightarrow e^+ \nu_e \mu^+ \mu^- d\bar{u}\gamma$, and
- $\gamma\gamma \rightarrow e^+ \nu_e \mu^+ \mu^- d\bar{u}\gamma$.

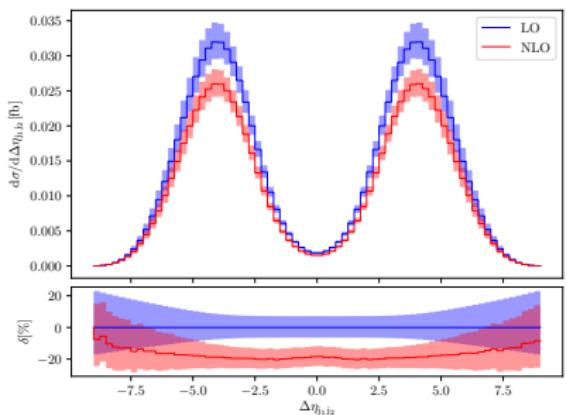
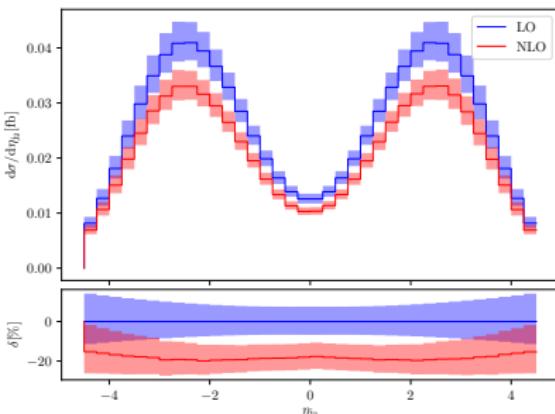
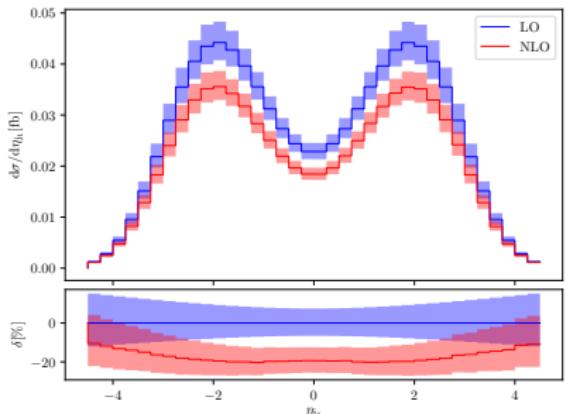
Integrated cross section

Integrated xs for $\text{pp} \rightarrow e^+ \nu_e \mu^+ \mu^- jj + X$ @ $\sqrt{s} = 13 \text{ TeV}$ for the fiducial PS volume:

LO [fb]	NLO [fb]	$\delta = \frac{\mathcal{O}(\alpha^7)}{\mathcal{O}(\alpha^6)} [\%]$
$0.2362^{+9.433\%}_{-8.022\%}$	$0.1899^{+8.356\%}_{-7.575\%}$	-19.6%

- Uncertainty is the range given by varying $\mu_F = M_W$ by (1/2,2)
- No dep. on $\alpha_s \rightarrow$ no dep. on μ_R
- **Huge corrections** ($4-5 \times$ larger than e.g. EW corr. for di-boson prod.) on the integrated cross section, larger than even like-sign W-scattering (-16%)
- Corrections are even larger in specific regions of p_T distributions

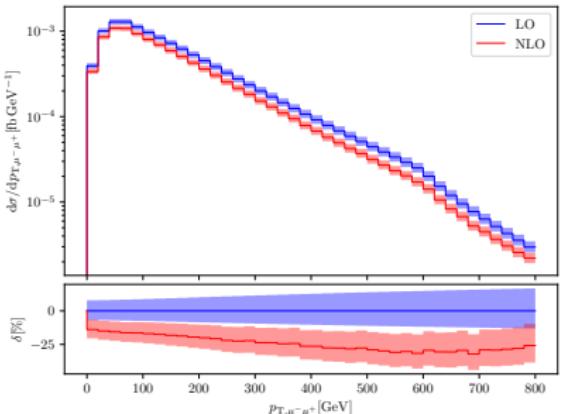
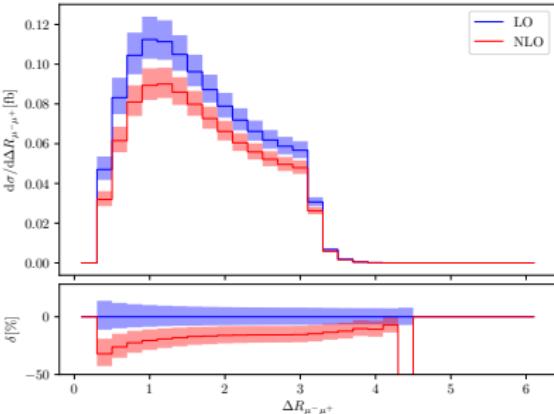
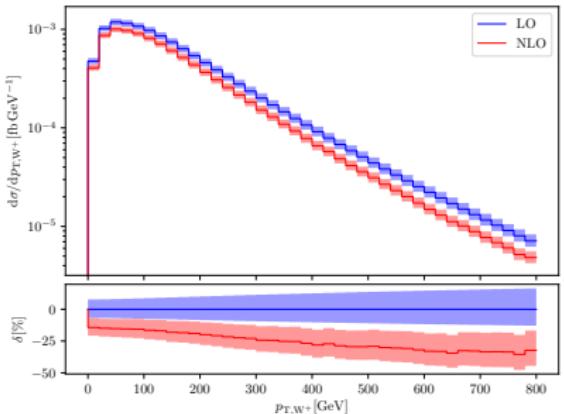
Jet pseudo-rapidities



- EW corrections flat in most PS regions
- Bands: large dependence on μ_F
- Peak at $\Delta\eta_{j_1 j_2} \approx 0$ suppressed because of $M_{j_1 j_2} > 500 \text{ GeV}$ cut:

$$\cosh \Delta\eta_{j_1 j_2} \approx \frac{M_{j_1 j_2}}{2 p_{T,j_1} \cdot p_{T,j_2}} + \cos \Delta\phi_{j_1 j_2}$$

Leptonic observables



$$\Delta R = \sqrt{\Delta\phi^2 + \Delta\eta^2}$$

- In p_{T,W^+} Sudakov logs further increase EW corrections
- $\Delta R_{\mu\bar{\mu}}$ is limited from above because $M_{\mu\bar{\mu}} \approx M_Z$ cut limits $\Delta\eta_{\mu\bar{\mu}} < 3.3$
- Kink at $p_{T,\mu\bar{\mu}} \approx \frac{2M_Z}{\Delta R_{\ell\ell}}$ caused by $\Delta R_{\ell\ell}$ cut

Summary

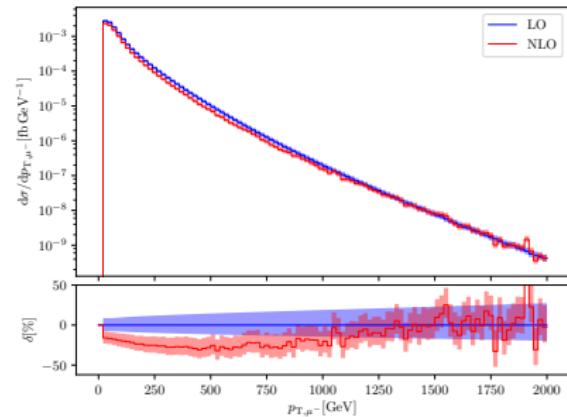
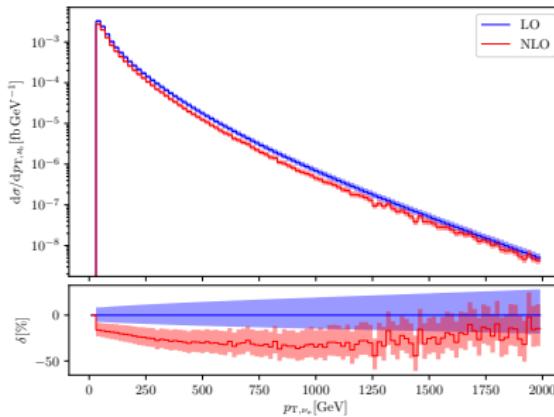
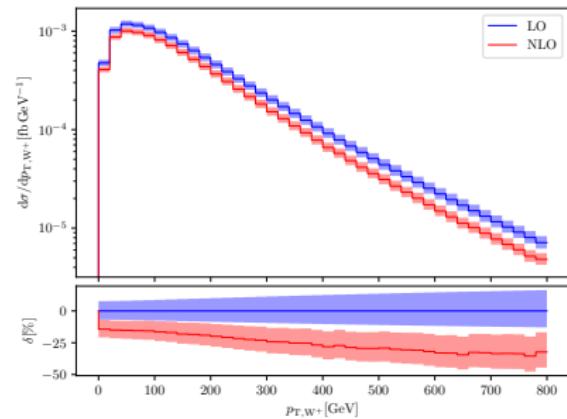
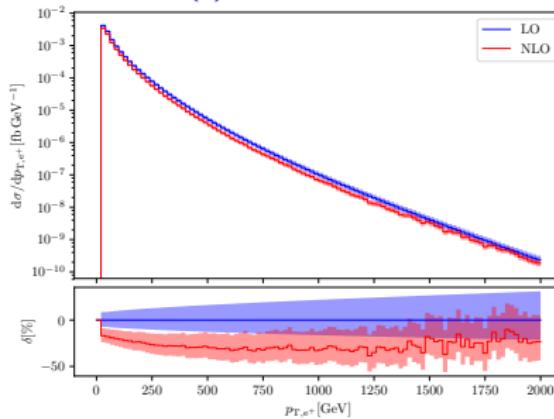
- Vector-boson scattering (VBS) important to constrain the actual Higgs-sector, complementary to Higgs-couplings measurements
- After W^+W^+ , W^+Z scattering is the next important channel for VBS
- Experiments are either measuring or already observing it
- EW corrections are available now, huge correction on the integrated cross-section: -20%

Acknowledgments

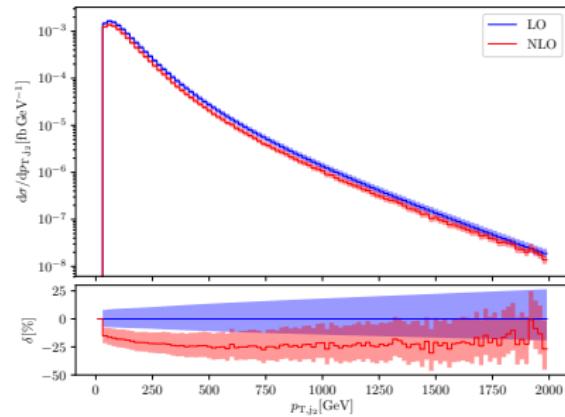
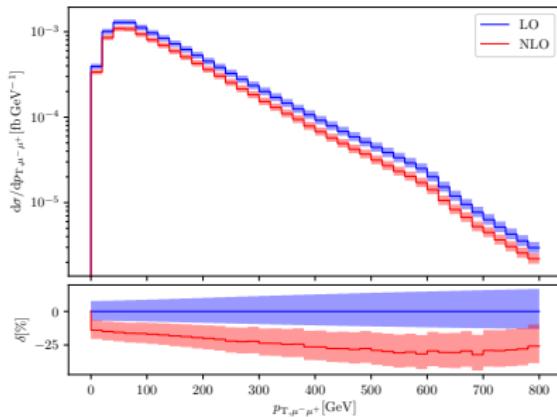
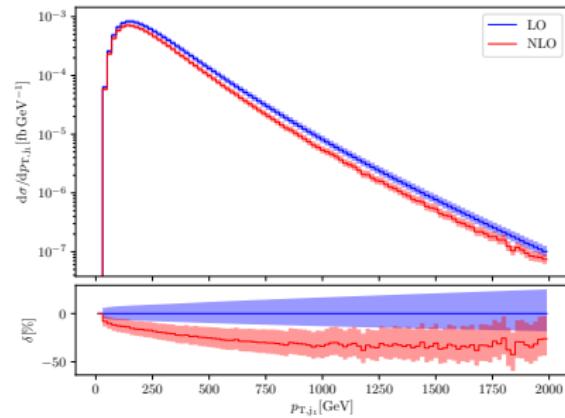
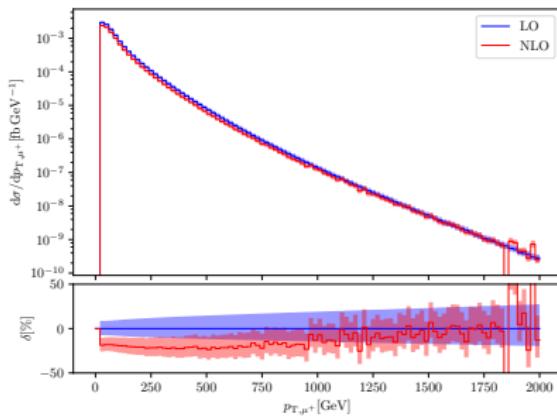
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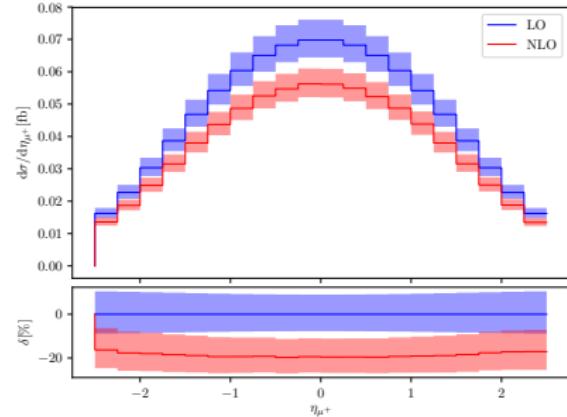
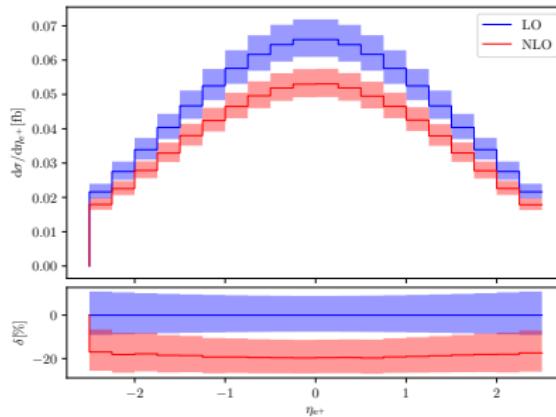
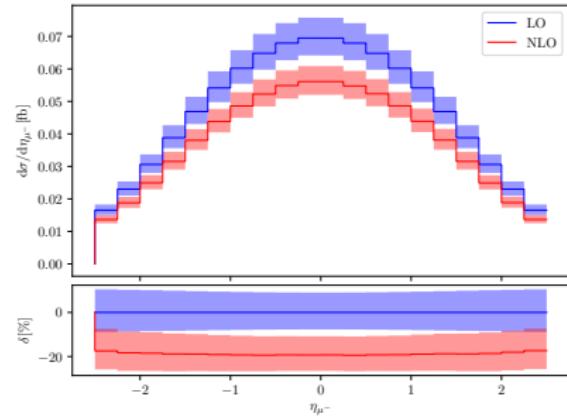
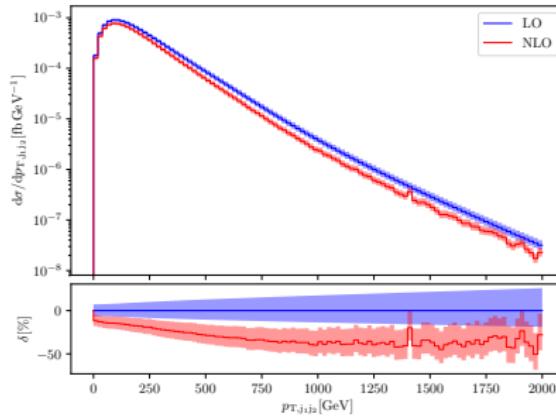
Distributions (I)



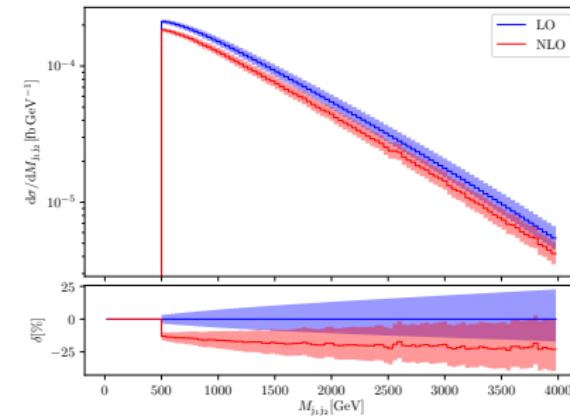
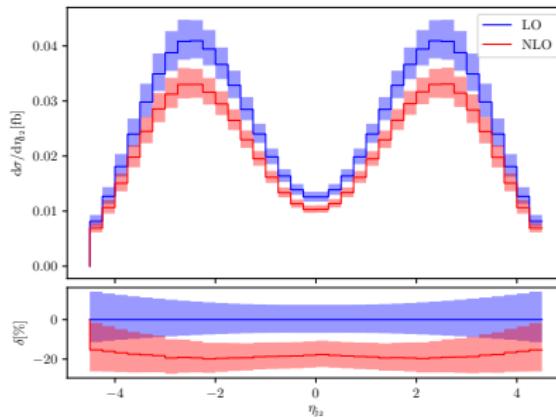
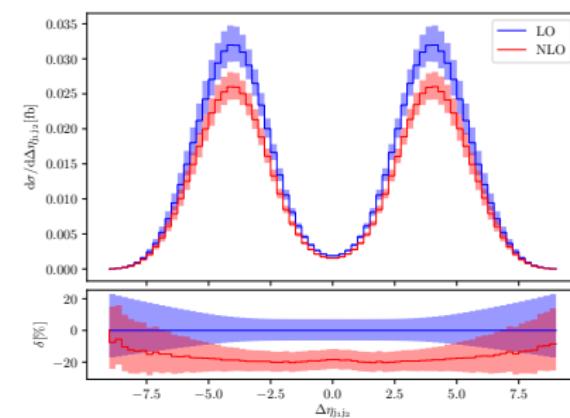
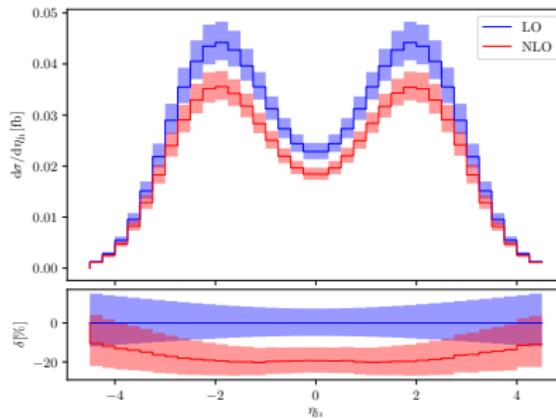
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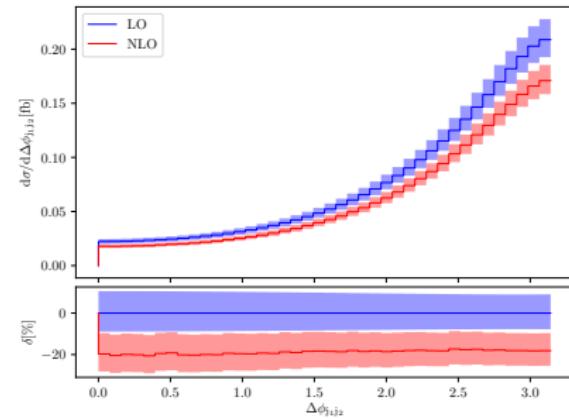
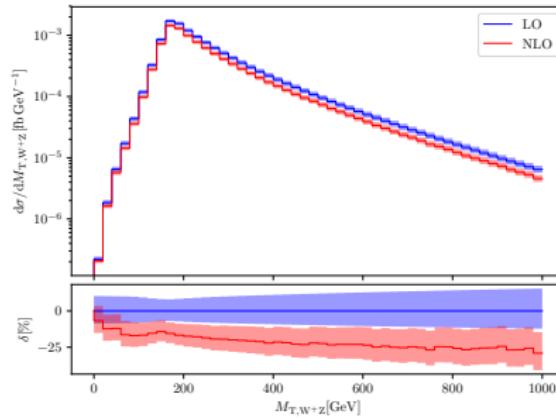
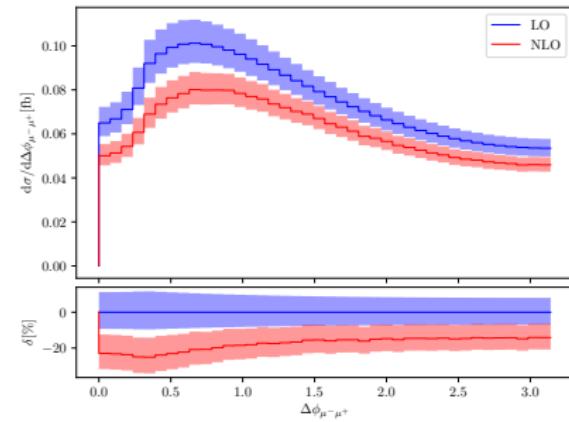
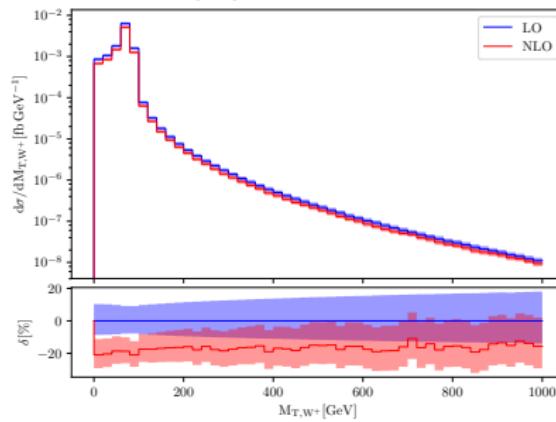
Distributions (III)



Distributions (IV)



Distributions (V)



Distributions (VI)

